

GY403 Lithostatic Stress Example Problem

Given:

Assume a 1cm^3 volume of continental crust is buried to a depth of 5 kilometers. The density of the material and all of the surrounding crust is 2.8g/cm^3 .

Calculate:

(1) The value of the lithostatic stress on the 1cm^3 cube of material in terms of kilobar.

(2) The stress gradient in terms of kilometers per kilobar.

From the description of the problem, and consideration of a fundamental physical law, we know the following:

$$a = \text{acceleration due to Earth's gravitational field} = 980 \text{ cm/sec}^2$$

$$\rho = 2.8\text{g/cm}^3$$

To solve for the stress:

$$F = ma$$

$$F = \rho Va$$

{V = volume of the overburden column}

$$F = \rho hba$$

{h = height of overburden column; b = area of base of column}

$$F = (2.8\text{g/cm}^3)(5.0 \times 10^5 \text{cm})(1.0\text{cm}^2)(980\text{cm/sec}^2)$$

$$F = 1.372 \times 10^9 \text{ g cm/sec}^2$$

$$F = 1.372 \times 10^9 \text{ dynes}$$

$$\sigma = F/A = (1.372 \times 10^9 \text{ dynes} / 1.0 \text{ cm}^2)$$

$$\sigma = (1.372 \times 10^9 \text{ dynes} / 1.0 \text{ cm}^2) \times (1 \text{ bar} / (1 \times 10^6 \text{ dynes} / \text{cm}^2)) = 1.372 \times 10^3 \text{ bar}$$

$$\sigma = 1.372 \text{ kilobar}$$

Lithostatic Stress Gradient

$$5.0 \text{ kilometers} / 1.372 \text{ kilobar} = 3.64 \text{ kilometers} / \text{kilobar}$$